

# Lessons from coding theory

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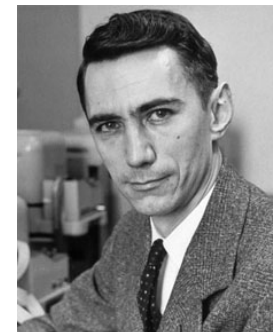
This talk is about

Error correcting codes

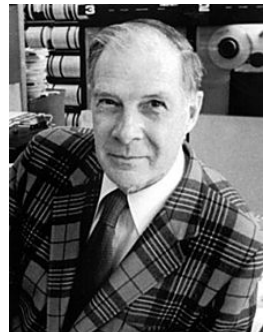
# You may be thinking

- What are error correcting codes?
  - Tools for protecting data from errors
- Classical solutions to problems in communication and storage...

*Isn't that a solved problem?*



Shannon



Hamming

# Actually...

- Lots of old problems **still open**
  - Fun to think about!
- Lots of **new applications** in communication and storage
  - Distributed storage is a big one
- But even if you are not into communication and storage
  - **Lots of applications everywhere!**



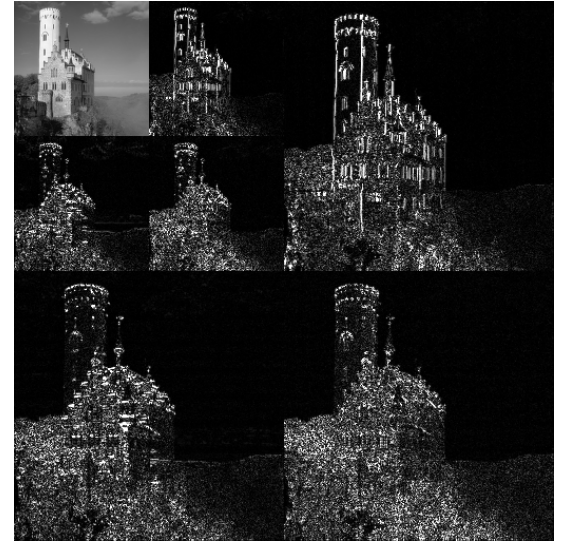
this is what this  
talk is really about.



# Common set-up

- We have some data
- It has some structure
  - which we don't control
- We want to take advantage of that structure
  - learn stuff about the data
  - do it efficiently

# Taking advantage of structure



linear  
measurements

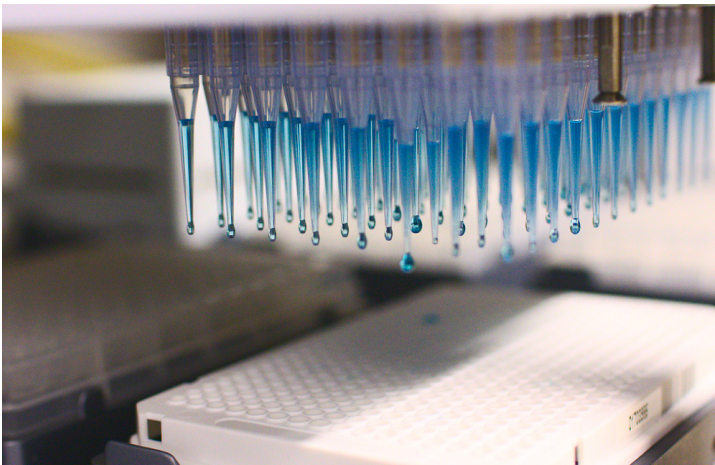
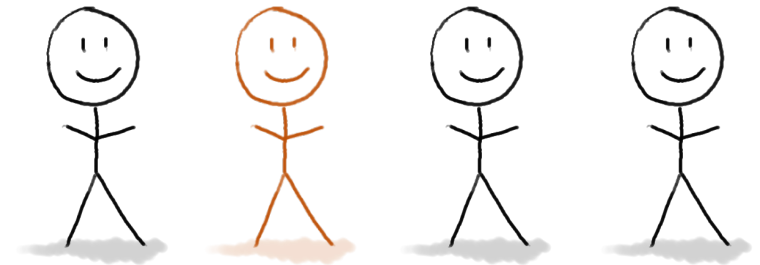


Compressed sensing/  
sparse recovery

# Taking advantage of structure

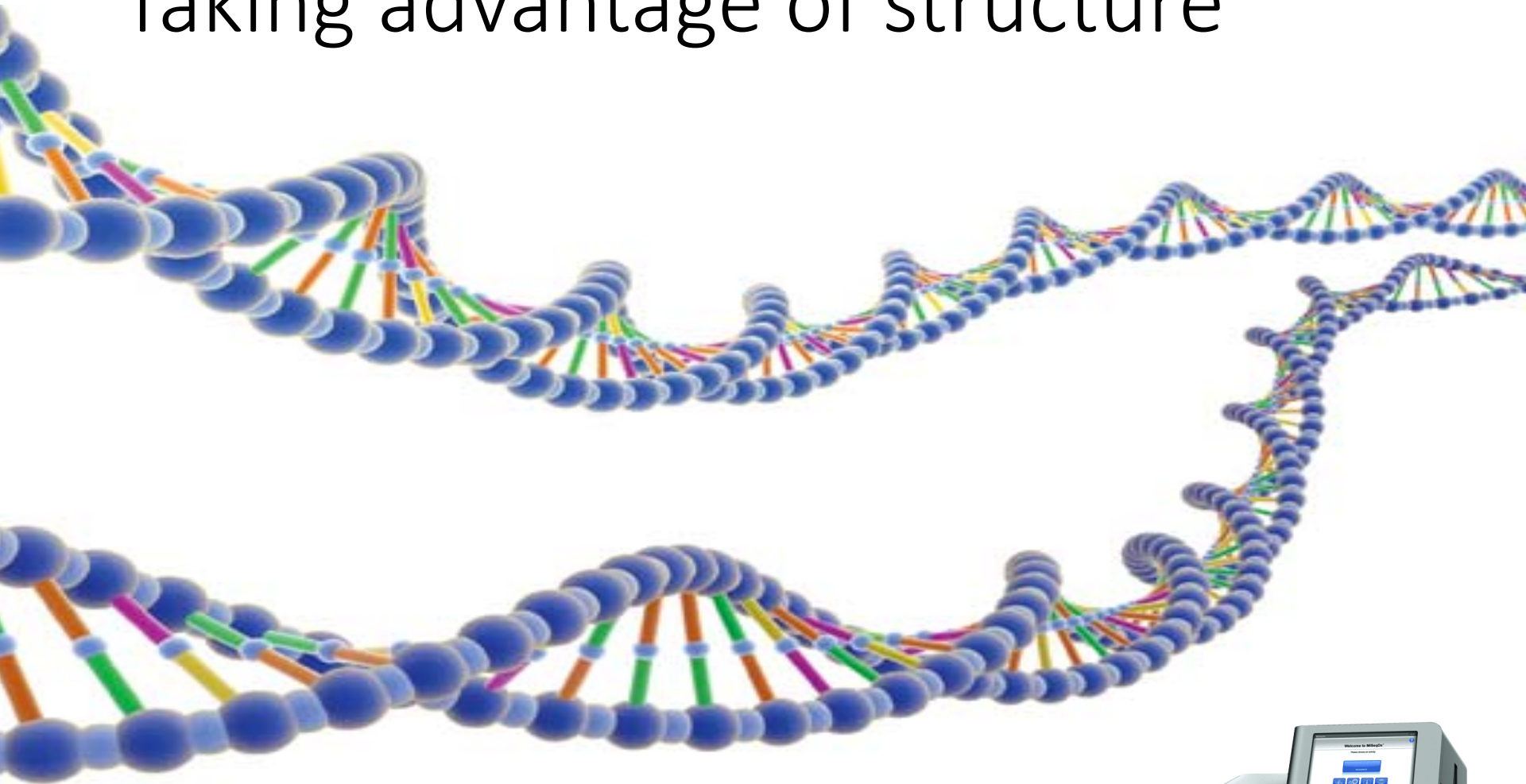


# Taking advantage of structure



High-throughput screening

# Taking advantage of structure



De novo sequencing

# etc...

- We don't control the structure
- We do (partially) control what happens to the data

# The other side of the coin

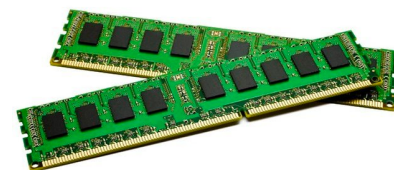
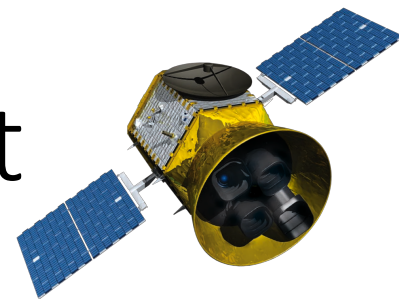
- We **do** control the structure
- We **don't** control what happens to the data



# Taking advantage of the most advantageous structure



# Taking advantage of the most advantageous structure



# Error correcting codes

are, by design, the **most advantageous** structure.

- Used in communication and storage since the 1950's
- Over half a century of beautiful work!

# Two questions

- Haven't we figured that out by now?
- What about this other stuff?
  - If we control measurements but not structure?



# As mentioned before

- Okay, so **we haven't really figured everything out.**
  - Coding and information theory for communication and storage is still a vibrant research area.



- But also!
  - Lessons from classical coding theory are relevant in a wide variety of these sorts of applications.

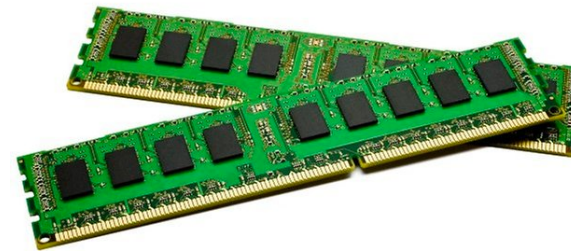


# My work

- Some of this:



- Some of that:



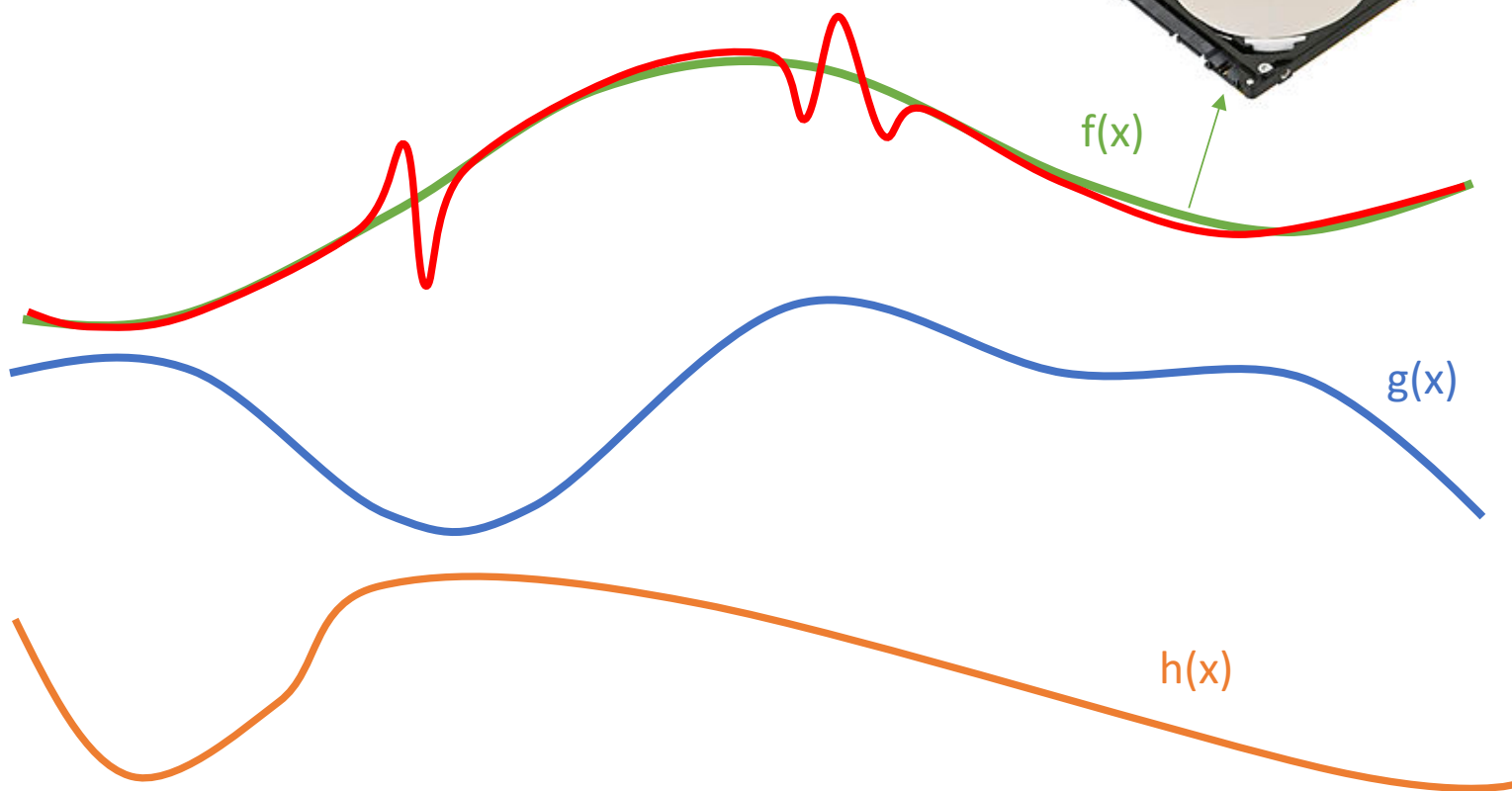
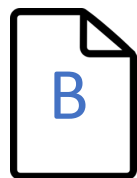
- Right now I'm really excited about the interplay between the two.



Disclaimer: many of the ideas I'll mention in the next five minutes are not mine and not new...but they are super cool!

# We don't have too much time so I'll just give one example

- Here's one very classical idea...



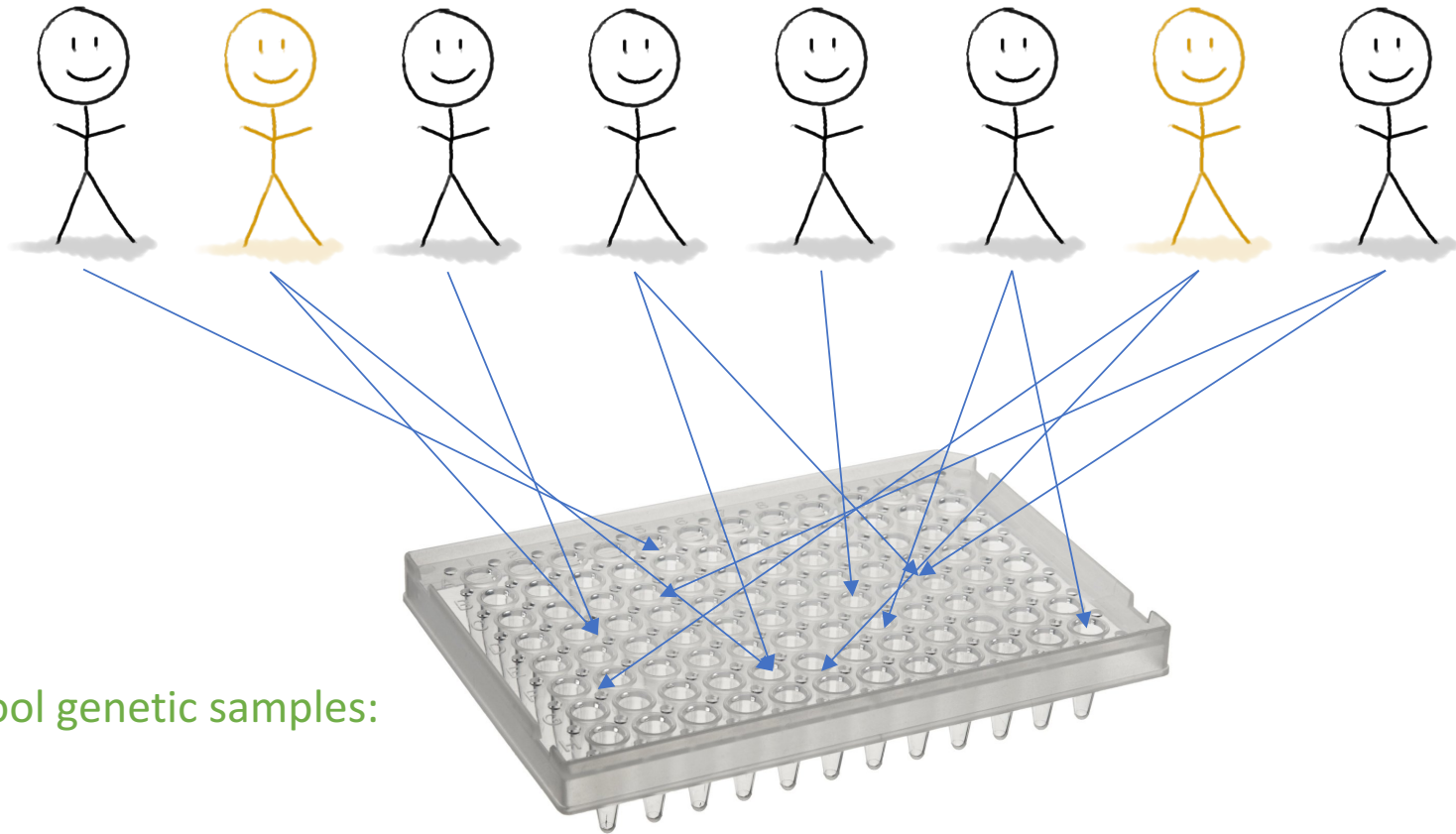
This is “Reed-Solomon encoding”

# Low-degree polynomials are the most advantageous structure\*

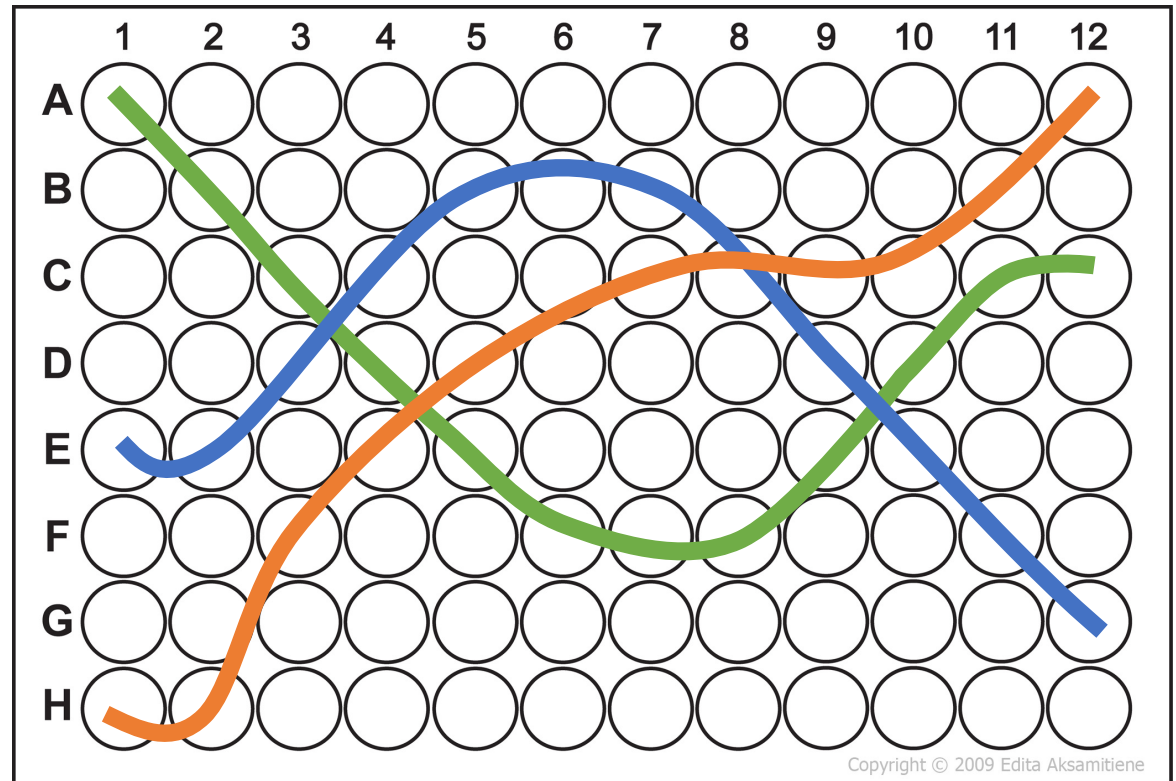
- Really nice combinatorial properties
- Admit really fast algorithms
- Used all over the place in communication and storage

# Not just in communication and storage

- High-throughput screening



# Pool samples according to low-degree polynomials

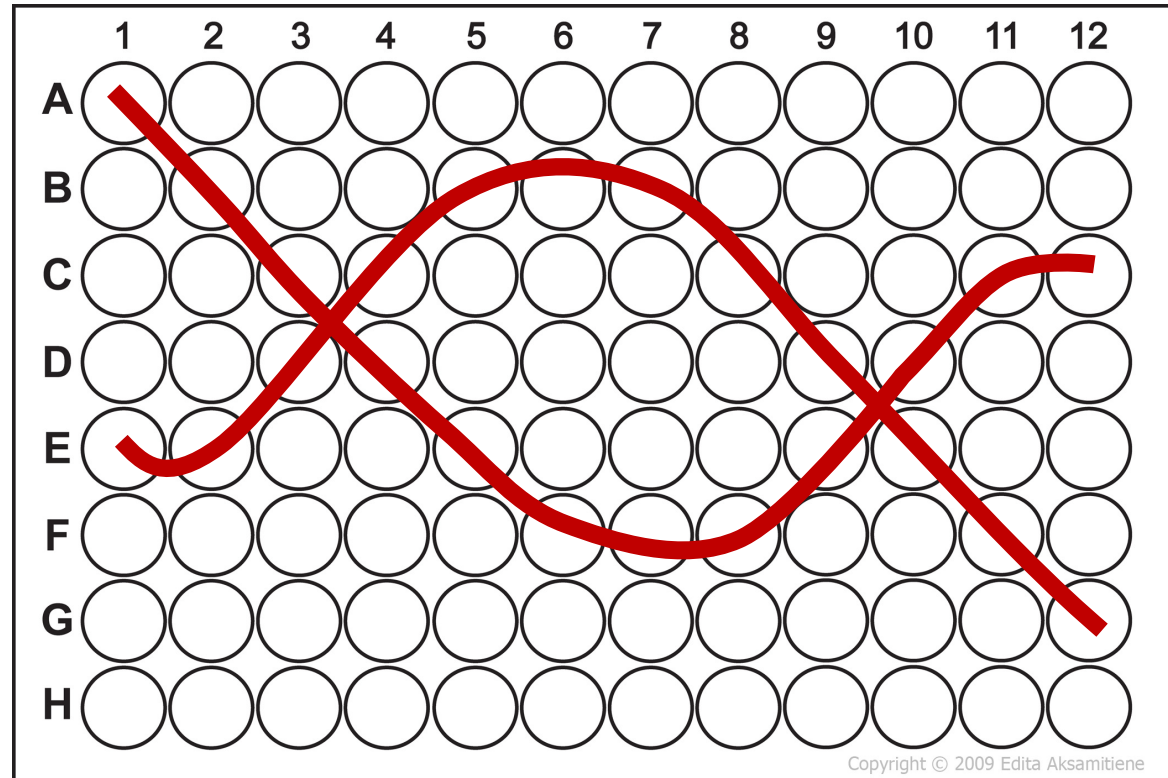
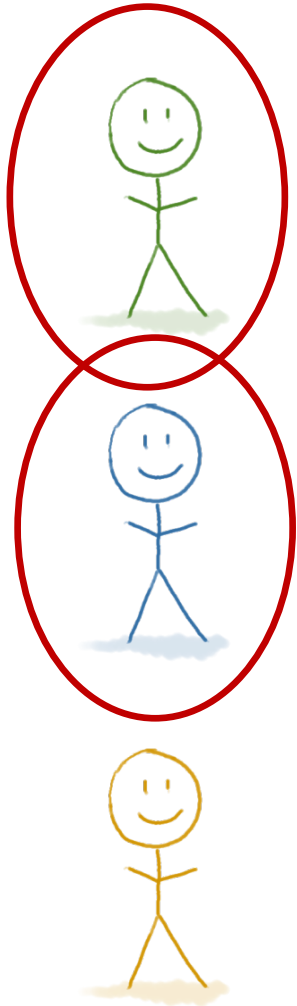
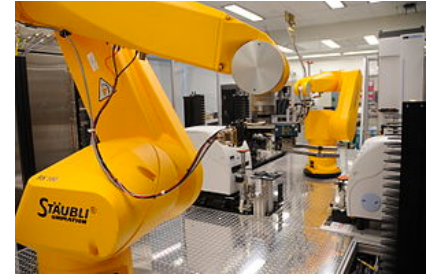


Imagine there are way more people  
than there are pools...

\*taking some  
artistic liberties

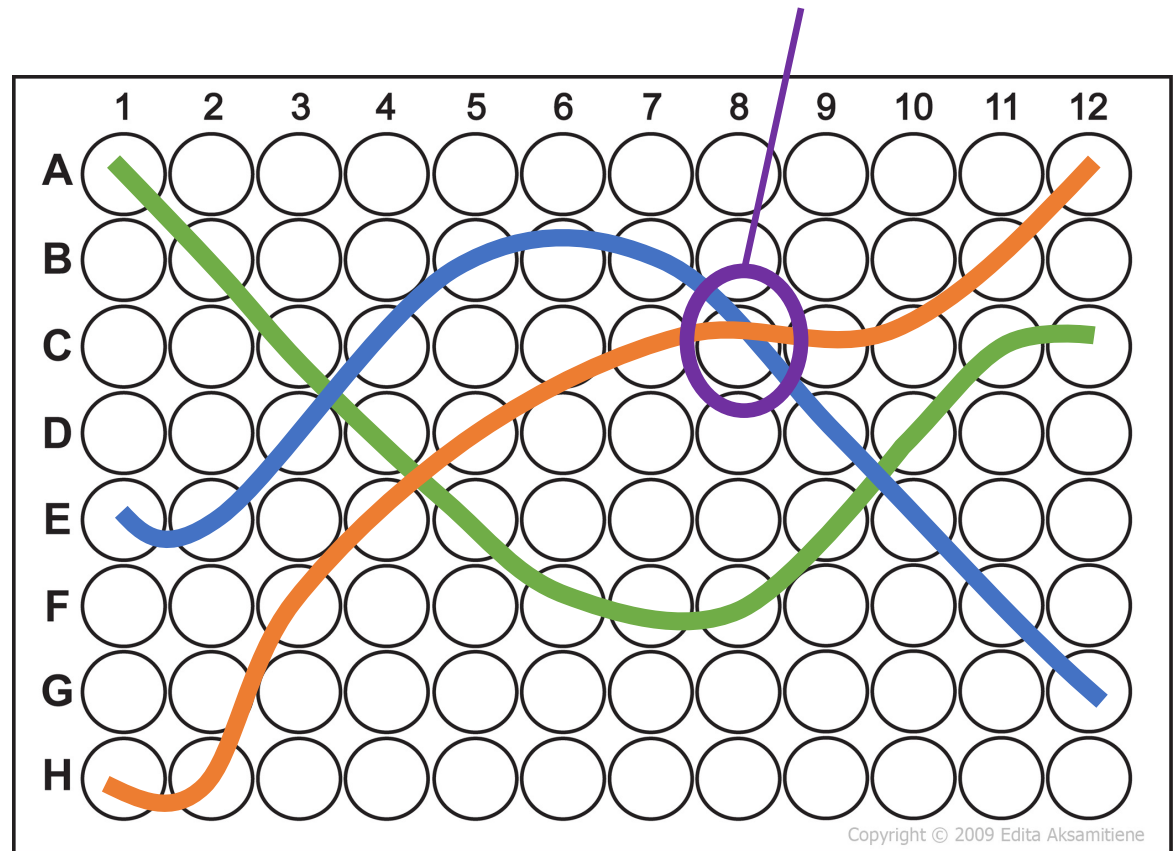
# Pool samples according to low-degree polynomials

- Not a new idea [Kautz & Singleton 1964]
- But making it work for modern problems comes with new challenges!



# Also, de novo genome sequencing

Sequence this pool altogether, get a bunch of reads...what came from what?



[Lonardi, Duma, Alpert 2013]  
[Duma, W., Gilbert, Ngo, Rudra, Alpert, Close, Ciardo, Lonardi 2013]

\*Taking even more  
artistic liberties...

Even if you don't control the structure...

- If you do control how you process the data, tricks like this work.
- Many examples in compressed sensing, group testing, streaming algorithms, ...
  - Cheraghchi, Gilbert, Indyk, Nelson, Ngo, Porat, Rudra, Strauss, ...



# Summary

- I think error correcting codes are cool.
  - And still an exciting area of research!
  - Talk to me later about distributed storage!
- But even if you don't care about communication, storage, or information theory,

error correcting codes are still cool.

# Thanks!

Contact me to talk more!

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Gates 468